

Comparative 3D Finite Element Stress Analysis of Straight and Angled Wedge-Shaped Implant Designs

Estevam Barbosa Las Casas, Eng, MSc, PhD¹/Paulo César Ferreira, Eng, MSc²/
Carlos Alberto Cimini Jr, Eng, MSc, PhD¹/Elson Magalhães Toledo, Eng, MSc, DSc³/
Luis Paulo da Silva Barra, Eng, MSc, DSc²/Mauro Cruz, DDS, MDSci, PhD⁴

Purpose: The goal of this work was to analyze the stress distribution in 2 wedge-shaped implant designs, straight and angled, by means of a 3-dimensional finite element method (FEM) stress analysis. **Materials and Methods:** A model was generated from computerized tomography of a human edentulous mandible with the implants placed in the left first molar region. The model included boundary conditions representing the muscles of mastication and the temporomandibular joint. An axial load of 100 N and a horizontal load of 20 N were separately applied at the tops of the implant abutments, and system equilibrium equations were used to find each muscle intensity force based on its position and direction. The mandibular boundary conditions were modeled considering the anatomy of the supporting muscle system. Cortical and medullary bones were assumed to be homogeneous, isotropic, and linearly elastic. **Results:** The stress analysis provided results in terms of normal maximum tensile (σ_1) and compressive (σ_3) stress fields. The stress distribution was quite similar for both designs, indicating a good performance of the angled design. **Conclusions:** Stresses in the angled implant were in general lower than in the straight implant, and the differences between the 2 designs studied were more relevant for the vertical load. No indication was found that angled implants of the type described generate stress-induced problems compared to straight implants. INT J ORAL MAXILLOFAC IMPLANTS 2008;23: 215–225

Key words: biomechanics, dental implants, dental stress analysis, finite element analysis

Different implant designs have been proposed and tested in an attempt to provide anatomic, prosthetic, esthetic, and functional solutions for partial or total tooth loss. The predictability of different implant systems is supported by many clinical studies.^{1,2} Recent systematic reviews^{3,4} have demonstrated a survival rate of approximately 96%, with no clinical differences among implant systems.⁵ Because of the variability of anatomic structures, implants

cannot always be placed in the desired number and location. For this reason, implants are sometimes placed in an inclined position.^{6–8} A common clinical procedure involves tilting the straight implant in cases where it is important to avoid anatomic structures such as the inferior alveolar nerve at the posterior region of the mandible or the maxillary sinus.⁶

To obtain the necessary prosthetic parallelism, tilted implants need angled abutments; this addition makes them geometrically similar to angled implants. The biomechanical behavior of these implants compared to vertically positioned implants has been the subject of previous works.^{8–11} The results of these works showed no clinical differences between tilted and vertically positioned implants. Angled implants have been proposed^{12–14} for better adjustment of the implant shape to the residual bone morphology, which could increase the applicability and functionality of the technique. The biomechanical behavior of such implants was analyzed and compared to the straight implant design.^{15,16} Many studies have focused on the biomechanical behavior and the clinical outcomes of angled implants, with

¹Professor, School of Engineering, Federal University of Minas Gerais, Belo Horizonte, MG, Brazil.

²Professor, Federal University of Juiz de Fora, School of Engineering, Juiz de Fora, MG, Brazil.

³Researcher, Computational Mechanics Coordination, LNCC, Petrópolis, RJ, Brazil.

⁴Director, Clinest - Clinical Center of Research in Stomatology; Researcher and Professor, São Leopoldo Mandic Research Center—School of Dentistry, Juiz de Fora, MG, Brazil.

Correspondence to: Dr Mauro Cruz, São Leopoldo Mandic Research Center, School of Dentistry, Av. Rio Branco, 2288/1205 Juiz de Fora, MG, 36016-310, Brazil. E-mail: mc@maurocruz.com

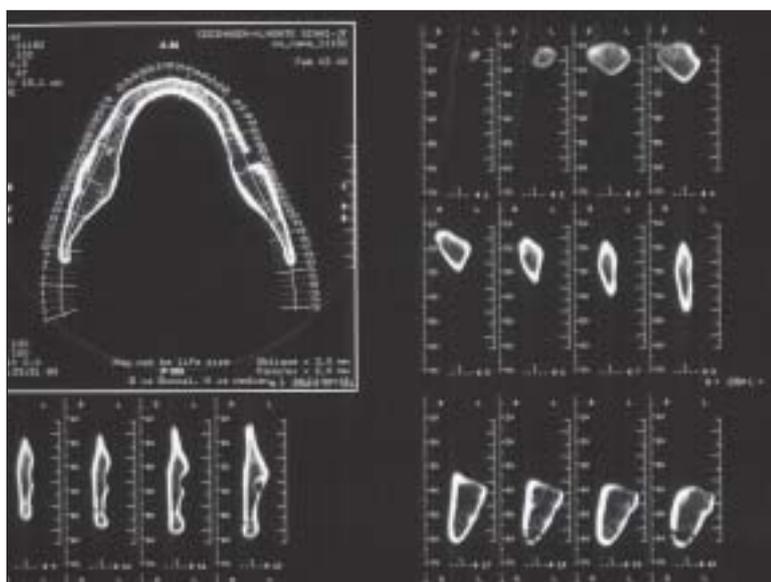


Fig 1a CT scan of the mandible.

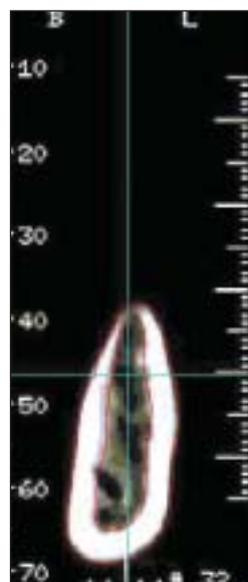


Fig 1b Cross section.

the angle situated on the body^{12,13,15,17} or between the implant and the abutments.^{7,9,18–24} Based on these studies, such implants have been recommended for anatomic, prosthetic, and biomechanical reasons. Different implant shapes and prosthetic concepts have been studied^{25–31} in the search for improved shapes to enhance the applicability of the implants. Angled¹⁶ and straight^{32–34} wedge-shaped implants are 2 of these alternatives.

The use of finite element method (FEM) in the mechanical analysis of dental implants has been described by many authors.^{7,15,26,28,35–42} This method presents a suitable degree of reliability and accuracy^{43–48} without the risk and expense of implantation, as pointed out by Cook et al.⁴⁹ To study a complex mechanical problem, FEM can be used to simulate the stress distribution, dividing the problem geometry into a collection of much smaller and simpler elements. Complicated geometric structures are thus converted into meshes in a computer set. The resulting models consist of elements, nodes, and predefined boundary conditions. Displacement and stress caused by loading on each node can then be calculated by a computer program.^{48,50} Image data obtained with the aid of computerized tomography (CT), 3-dimensional scanning (3D), or magnetic resonance imaging is used to generate the FEM model and the mesh necessary for the analysis. The quantitative data obtained by the stress analysis can be correlated⁵¹ with the physiologic bone threshold.^{52–57}

The purpose of this work was to analyze and compare stress distribution around 2 implant shapes, straight and angled, under vertical and horizontal loading by means of a 3D FEM stress analysis.

MATERIALS AND METHODS

The geometric model generation was based on previous works with the development of a model of implants fixed to an edentulous mandible.^{32,34,43,46}

Modeling

The model of the human mandible was generated based on CT (Pro-Speed, GE, Medical Systems, Fairfield, CT; Fig 1). Sections of the CT scan were digitalized and used as input for the Ansys pre-processor (Ansys, Canonsburg, PA). Coordinates of the points in each of the available sections served as a basis for the generation of lines (Fig 2a), defining the contour surfaces (Fig 2b) and resulting in a solid model of the mandible, include internal boundaries between the cortical and medullary bone.

The implants considered had a wedge-shaped basic shape with either a straight long axis or an angled long axis (Bioform implant; Maxtron Co, Juiz de Fora, MG, Brazil). The straight implant had a length of 13 mm and a diameter of 4 mm (Fig 3a). The angled implants are of 2 different types, lateral and frontal angled. The lateral angled implant has a long axis inclined toward the narrowest face of the body (named the “lateral face” of the implant) 4 mm from the platform, with 3 different slopes (25 degrees, 40 degrees, 55 degrees; Fig 3b). The frontal angled implant has a deviation of the long axis toward the largest face of the body (named the “frontal face” of the implant) 4 mm from the platform; it also is available in 3 different slopes (25 degrees, 35 degrees, 45 degrees; Fig 3c). Both are designed to contour anatomic structures such as the sinus, inferior alveolar

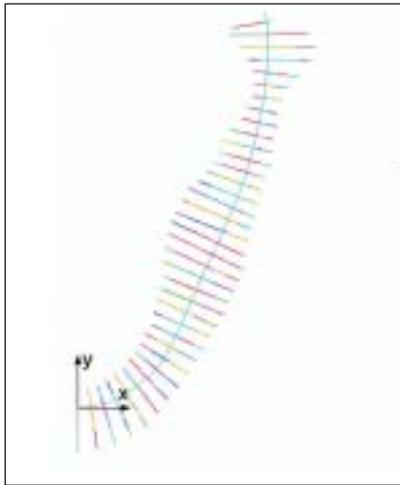


Fig 2a Contour lines.



Fig 2b The use of contour lines to model surfaces.

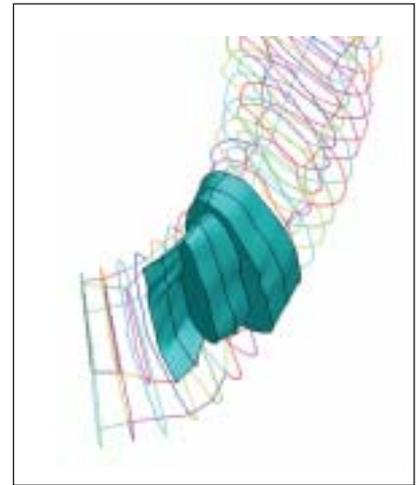


Fig 3a Straight wedge-shaped implant.



Fig 3b Laterally angled wedge-shaped implant.



Fig 3c Frontally angled wedge-shaped implant.

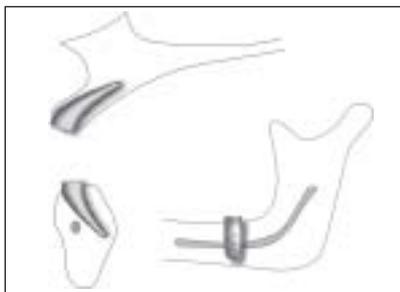


Fig 4a Clinical indications for the use of angled implants.

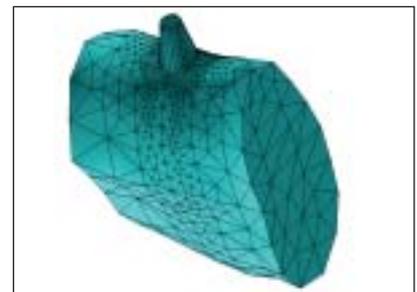


Fig 4b Detail of the model in the first molar region.

nerve and mental foramina and to enhance prosthetic, esthetic, and biomechanical conditions (Fig 4a). The subject of this study was a front-angled implant with a diameter of 4 mm, a length of 14 mm, and a slope of 35 degrees. The dimensions of the considered implants were chosen to match previously reported FEM studies. All implants had 3 notches on each side of the largest face of the body (Fig 3).

Information on the dimensions of the implants was provided by the manufacturer. The situation simulated was the placement of an implant in the first

molar region (Fig 4b). A layer of cortical bone of 2 mm was modeled around the implant neck, and the body was modeled as being embedded in medullary bone and surrounded by a 1-mm layer of compact bone.³⁵ Thus, the model was a simplification of the more complex configuration observed in actual cases.¹ The straight implant was positioned vertically through the mandible, while the angled implant was placed with the straight apical portion of the body tilted toward the buccal surface of the mandible, within the cortical layer (Fig 5).

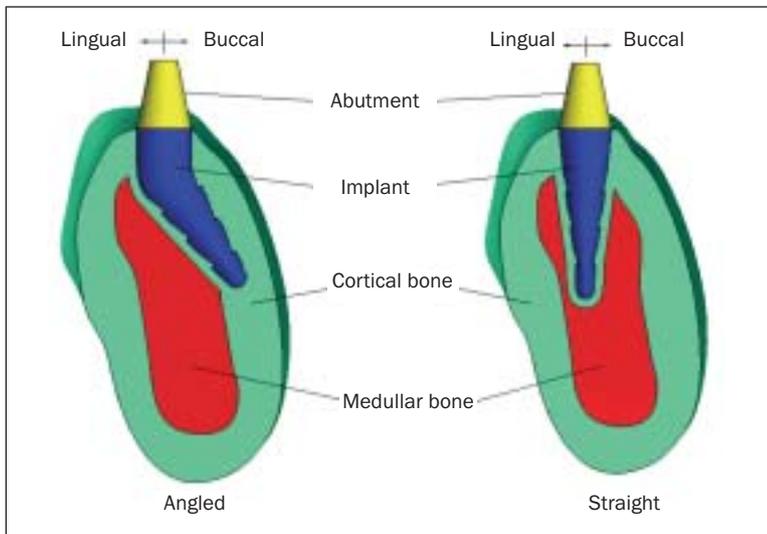


Fig 5 Each implant in the planned position.

Region	No. of elements		No. of nodes	
	Straight	Angled	Straight	Angled
Implant-abutment	17,897	17,902	26,552	26,389
Molar region	34,188	34,426	47,263	47,245
Complete model	53,057	53,790	75,941	76,358

The geometric model was meshed with tetrahedral isoparametric quadratic elements consisting of 4 triangular faces, 4 vertices, and 10 nodes. The mesh used was defined through refinement tests. The convergence of the results was verified in the cervical region of the implant, which is subjected to the highest stress levels. The mesh used had around 62% of the elements concentrated in the region where the implant was placed (Table 1).

Vertical loads (axial) of 100 N and horizontal loads (90 degrees to the vertical) of 20 N were applied at the central node in the upper surface of the abutment^{15,27,38} (Figs 6a and 6b). The solid model resulting from the Boolean intersection of the implant and mandible represents the assumption of complete osseointegration, restricting any relative displacement between implant and bone.

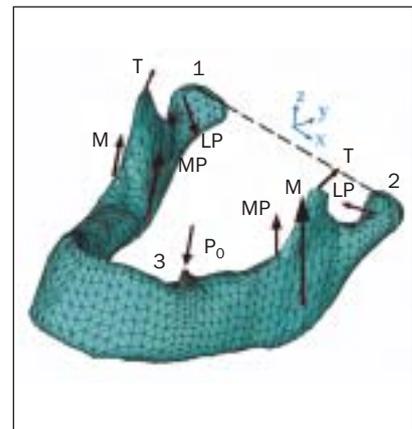
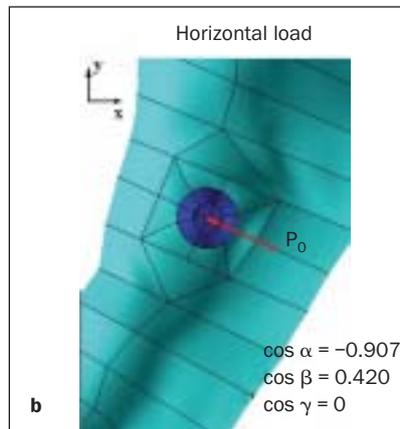
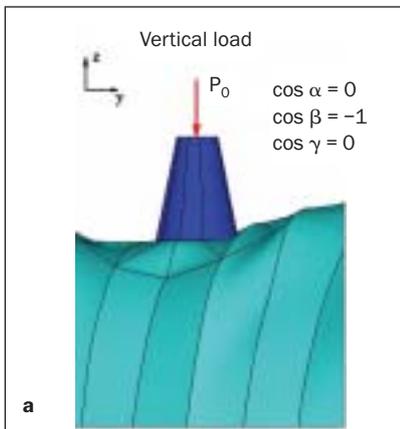
Load and Support System

The final model was supported by force vectors simulating the actions of the muscles of mastication (masseter, medial pterygoid, lateral pterygoid, and temporalis) and the temporomandibular joints⁵⁰ (Fig 7). The acting forces generated by the mastication muscles and transferred to the vectors were calculated based on the transverse sections, as proposed by Inou et al.⁴⁶ The data obtained from this reference indicate the following relationships between the muscle actions, based on the average size of their cross-sectional areas at the mandibular interface:

- M = 1.72 LP
- T = 0.99 LP
- MP = 1.15 LP

where M is the masseter, LP is the lateral pterygoid, T is the temporalis, and MP is the medial pterygoid. For horizontal and vertical loading, both condyles were completely restrained. The values of muscular forces for both loading cases were determined by the moment equilibrium equation around the axis connecting the condyles, which is given by the expression:

$$(\vec{r}_M \times 2\vec{M} + 2\vec{MP} \times \vec{r}_{MP} + 2\vec{LP} \times \vec{r}_{LP} + 2\vec{T} \times \vec{r}_T + \vec{P}_0 \times \vec{r}_p) \cdot \vec{e} = 0$$



Figs 6a and 6b Load application.

Fig 7 Directions of the muscular forces and boundary conditions.

Table 2 Distance Vector Components in mm			
Vector distance	Direction		
	X	Y	Z
r_M	0.0	28.07	33.01
r_T	0.0	30.61	5.27
r_{LP}	0.0	9.56	6.31
r_{MP}	0.0	27.67	38.97
r_{P_0}	0.0	80.63	23.89

Table 3 Director Cosines of the Resultant Muscular Forces (Right Side)			
Muscle	Cosine		
	α	β	γ
Masseter	-0.043	-0.011	0.999
Medial pterygoid	0.587	-0.165	0.792
Lateral pterygoid	0.714	-0.692	0.106
Temporalis	-0.325	0.219	0.920
P_0 horizontal	-0.907	0.420	0
P_0 vertical	0	-1	0

Table 4 Resultants of the Muscular Forces for Vertical and Horizontal Loads				
Load	Resultants of the muscular forces			
	M	MP	LP	T
Vertical (100 N)	49.251	32.626	28.634	28.348
Horizontal (20 N)	1.787	1.195	1.039	1.029

Table 5 Elastic Materials Properties			
Material	Elasticity modulus	Poisson's ratio	References
Cortical bone	13,700 MPa	0.30	15, 27, 29, 35, 37, 38, 49
Medullary bone	1,370 MPa	0.30	27, 35, 37, 38
Titanium	110,000 MPa	0.33	29, 39

Variables r_M , r_{MP} , r_{LP} , and r_T and r_{P_0} are the distance vectors from the load application points of the muscles forces M, MP, LP, and T and of the axial implant loads P_0 to the (1-2) axis passing through the tops of the condyles, respectively. The same equation was used for axial and horizontal loads, with the distance varying accordingly. The symbol \times denotes the vector product, the symbol \cdot denotes the inner vector product, and \vec{e}_1 is the unit vector in the condylar axis direction. The positions of the muscular forces and axial load are given in vector form in Table 2. Under the assumption of symmetric muscular loads, asymmetry is generated by the reaction forces in the condyles. Moment equilibrium in the axis, obtained by the finite element analysis, results in different condyle forces and thus an asymmetric stress distribution in the model.

The locations and directions of the muscle force vectors were obtained from the literature.^{46,47} Their resultants were considered to be acting on the centroid of the elements included in the areas of muscular action. Force directions are described in terms of director cosines, as given in Table 3. Obtained values for each muscular force, considering both vertical and horizontal loads, are listed in Table 4. Elastic properties for cortical bone, medullary bone, and titanium were extracted from the current literature and are listed in Table 5. Thicknesses of the cortical and medullary bone were based on the CT sections of the mandible. The bone was assumed to be isotropic, homogeneous, and linearly elastic, which allowed immediate extrapolation of the obtained results for different load levels.

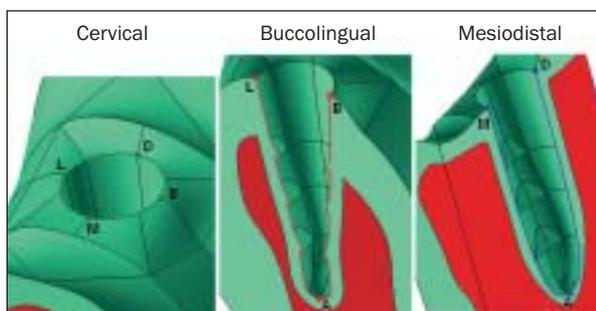


Fig 8 Straight implant contour lines illustrating the stress path.

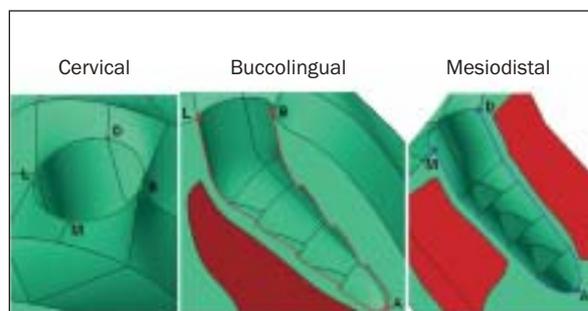


Fig 9 Angled implant contour lines illustrating the stress path.

The analyses were done using the commercial finite element code Ansys and processed in a Pentium 4 personal computer.

RESULTS

Principal stresses were obtained from the analysis, allowing the consideration of maximum compressive and tensile stresses, as bone behavior under tension and compression is essentially different. Figures 8 and 9 show points distributed along the implant-bone interface at a cervical, a buccolingual, and a mesiodistal section used to plot maximum (σ_1) and minimum (σ_3) principal stresses. Along the paths shown in Figs 10 and 11, graphs were generated to make comparisons between the maximum (σ_1) and minimum (σ_3) principal stresses for both implant designs under vertical and horizontal loads (Figs 10 to 13).

Under vertical load, the straight implant presented a high compressive peak stress concentration on 1 side of the neck and a smooth distribution along the body (Figs 10 and 11), which was in agreement with previously reported results.^{32,34} For the angled implant under vertical load (Figs 10 and 11), the stress distribution was quite similar. The largest tensile stresses occurred at the larger curvature region (buccolingual line) near the cervical area, while the highest compressive stresses occurred on the cervical line at the lingual side. A similar pattern was observed for horizontal loading (Fig 13) in case of compressive stresses, although different values were found.

On the mesiodistal cross section, no considerable differences were observed for either design, but the maximum compressive stress distribution showed a slight increase in the region around point A of the angled implant compared to the straight implant. Differences were noted for horizontal and vertical loading. Tables 6 and 7 present the principal stresses

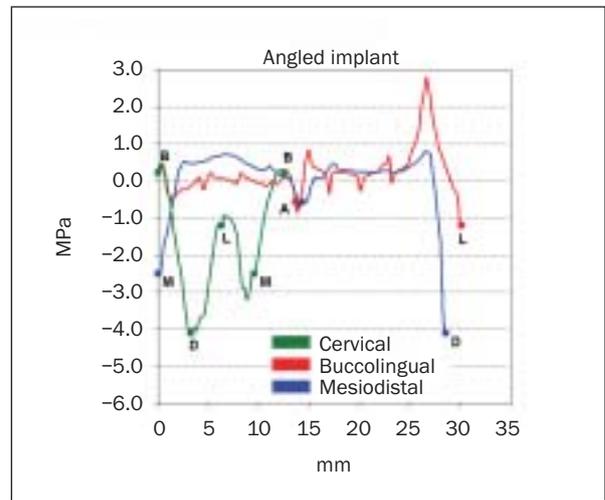
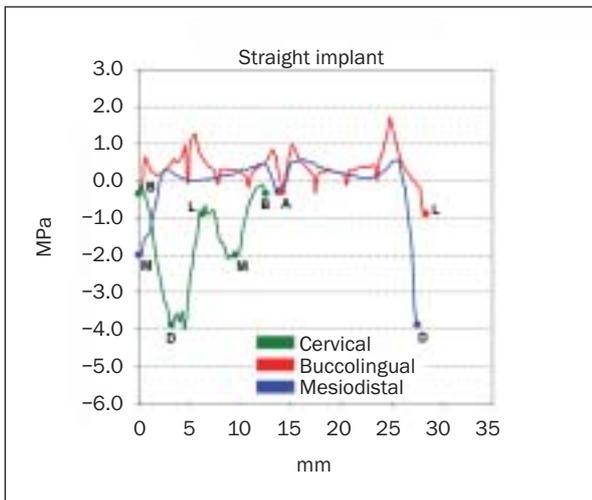
in the sections indicated in Figs 8 and 9, summarizing the obtained results for vertical and horizontal loading. More pronounced difference was observed for vertical loading at cervical point B. The difference reached a factor of 2.25 for compressive stresses and, for horizontal loading, a factor of 1.95, with higher values for the straight implant in both cases. In general, stresses in the angled implant were lower than for the straight model, with the exception of point A under vertical loading.

DISCUSSION

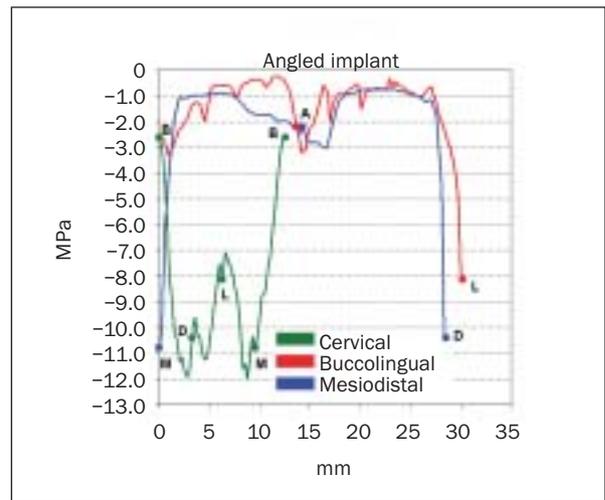
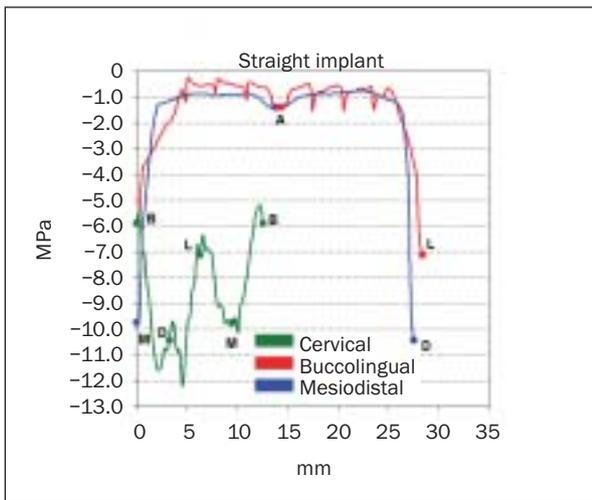
The purpose of this investigation was to provide an analysis between 2 different geometric configurations of implants and to compare their biomechanical behavior. Even with the simplifications made (homogeneity of the bone quality, symmetric muscle action, complete osseointegration, and static load) the model results may be very close to actual situations observed in clinical studies.^{39,43-45,47}

Many of the assumptions adopted in the current model should be taken into account in the analysis of the results. Complete osseointegration is not observed in clinical studies, as the level of osseointegration is highly variable. In a 3D finite element analysis of osseointegration percentages and patterns on implant-bone interfacial stresses, Papavasiliou et al⁴⁰ concluded that different degrees of osseointegration do not affect the stress levels or distributions for axial or oblique loads. So, fixing a value of 100% in a comparative study does not affect the conclusions.

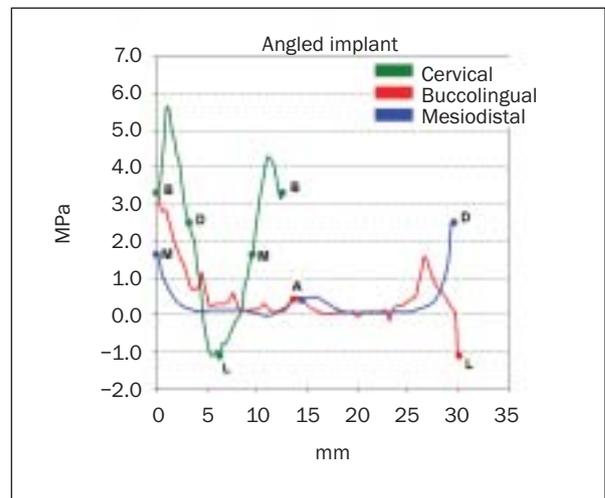
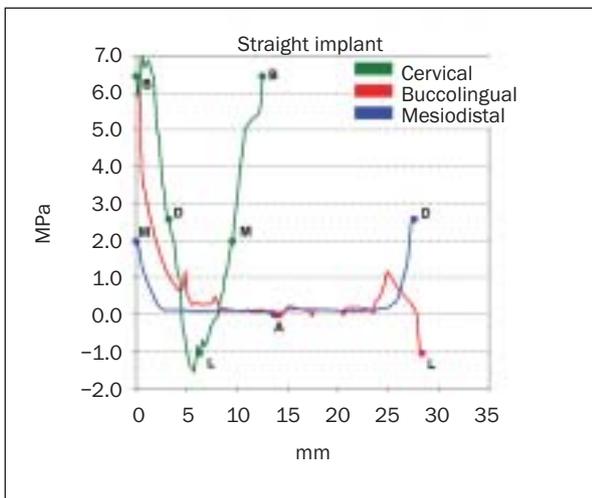
Mesh density is another relevant parameter. As the surfaces are curved, improving the mesh usually improves the results for the discrete model (increasing the accuracy in regions of high stress gradients). Another effect of increasing the number of elements is to reduce sharp angles created artificially by the process of substituting the model with the mesh,



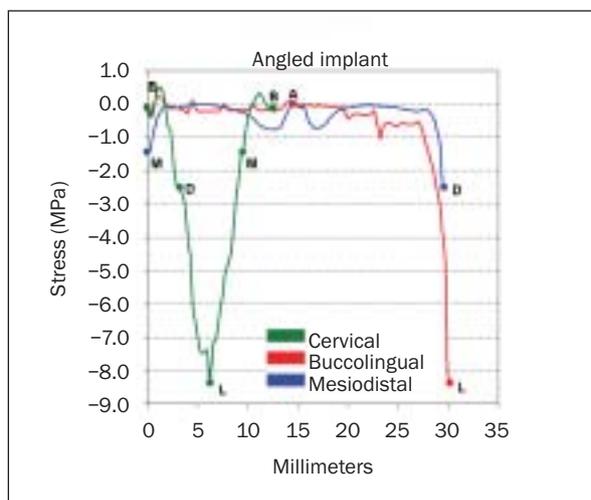
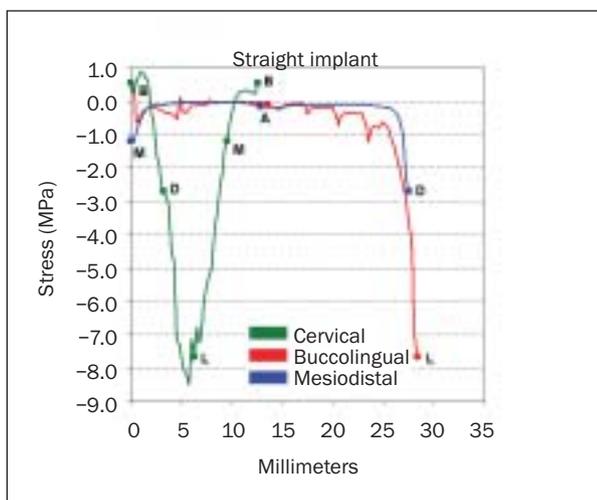
Figs 10a and 10b Major principal stresses along previously defined paths—vertical load (σ_1).



Figs 11a and 11b Minor principal stresses along previously defined paths—vertical load (σ_3).



Figs 12a and 12b Major principal stresses along previously defined paths—horizontal load (σ_1).



Figs 13a and 13b Minor principal stresses along previously defined paths—horizontal load (σ_3).

	Straight implant		Angled implant	
	σ_1 (MPa)	σ_3 (MPa)	σ_1 (MPa)	σ_3 (MPa)
Cervical				
Buccal	-0.34	-5.90	0.21	-2.62
Lingual	-0.88	-7.12	-1.21	-8.13
Mesial	-2.00	-9.74	-2.52	-10.78
Distal	-3.89	-10.44	-4.11	-10.41
Apical	-0.29	-1.40	-0.56	-2.20

	Straight implant		Angled implant	
	σ_1 (MPa)	σ_3 (MPa)	σ_1 (MPa)	σ_3 (MPa)
Cervical				
Buccal	6.44	0.54	3.30	-0.11
Lingual	-1.06	-7.67	-1.12	-8.37
Mesial	1.97	-1.18	1.63	-1.44
Distal	2.55	-2.68	2.48	2.51
Apical	0.00	-0.11	0.39	0.00

reducing artificial peak stresses by improving the representation of the actual geometry.

The consideration of a limit for the interface resistance between bone and implant, which was not included in the present model, is an interesting topic for future models. It requires nonlinear treatment of the problem of contact and fracture at the implant-bone boundary. In recent years, studies have shown that a more precise consideration of the physical processes in finite element models used in dental biomechanics can lead to more reliable results.^{27,43,46,48} The modeling of the whole mandible, with the muscles, temporomandibular joints, and the supporting system can bring the model closer to reality.^{43,46} Three-dimensional modeling, special attention to boundary conditions, the use of a fine mesh with an appropriate number of degrees of freedom—all these factors contribute to the precision of the computational results.^{43,46,48,49}

The modeled muscular force action at the bone surface generated stresses as high as those obtained around the implant, as shown in previous studies.^{32,34} This fact provides a qualitative way of comparing the obtained stress levels and suggests that modeling of the whole mandible is important.⁴³⁻⁴⁶

Comparative FEM stress analyses between different implant designs or different implant prosthetic concepts under the same conditions have been previously reported.^{26,27,30,36,38,42} They have often been used to compare new designs to classical implant forms. Comparisons under different modeling conditions can serve as a reference but do not provide conclusive proof. However, different studies have presented comparisons with the Brånemark system. This system can be used as a reference, as it has been thoroughly studied and has provided good clinical results.^{26,29,36}

In previous works, Cruz³² and Cruz and et al³⁴ studied the biomechanical behavior of the wedge-shaped straight implants. These works showed how the straight wedge-shaped implant relates to the Brånemark system in terms of biomechanical behavior. Therefore, the straight wedge-shaped implant can serve as a reference for comparison with the angled wedge-shaped implant, and the results presented here can then indirectly establish the relationship between the behavior of the wedge-shaped angled design and the usual standard. The effect of having an angled design rather than a straight shape can also be studied in terms of stresses.

In the present study, stresses were generally lower in the angled implant than in the straight implant, indicating that stress-induced bone resorption should not be more critical in this design than in more usual straight implants. This finding was unexpected, as the indication for such implant designs comes not from the need to reduce stresses but from occasional anatomic difficulties in the use of more traditional solutions.^{12,13} The larger differences in peak stresses were for vertical loading for compressive stresses on the lingual side of the cervical region of the straight design. As in the case of horizontal load, this increase was also larger for the straight implant. Interpretation of the numerical results should take into account that in normal function, during mastication, the vertical components of the loading are higher than the horizontal components, while in parafunction, horizontal loads can be dominant.

Canay et al¹⁵ reported a 2-dimensional analysis of vertical and angled implants of the ITI Bonefit system. Unlike the design modeled in the present study, the inclined part of the implants in the Canay et al study was outside the bone. The designs were recommended for 2 quite different problems and submitted to different stresses. The obtained results were not conclusive in terms of the clinical performance of the angled implant, even though they indicated that angled implants seem to provide an effective solution that does not compromise the stress levels developed in the bone. The same observation was made by Clelland et al⁹ with respect to angled abutments, by Schroeder et al¹² and Sutter et al¹³ with respect to angled implants, and by Satoh et al⁷ with respect to both.

Conversely, the angled implant can provide better structure for the prostheses^{17,23} by keeping the angle of the implant inside the bone and loading to a smoother stress distribution. It also often allows bicortical implant fixation when the implant is placed in the mandible with the apex of the implant resting in the buccal cortex. Data based on patient observation would be required to assess the comparative advantages of this design in specific clinical situations.

Rieger et al²⁶ and Inou et al,⁴⁶ based on previously published physiologic thresholds, reported that in their experiments bone resorption occurred in regions where the stress concentration was under or over the physiologic limits. In regions where the stress was within those limits, the bone maintained its morphology. The results of the present investigation indicated that both designs analyzed showed stresses in the same stress range (ie, within the physiologic levels).^{55,56}

A shape that takes peak stresses away from the bone crest should be chosen for clinical use, as stated by Akpınar et al.³⁷ This did not totally occur with the present designs, but the stress distribution pattern of this analysis showed values in the neck of the same magnitude as those at the muscle insertion, as previously described by Cruz³² and Cruz et al^{34,57} for the straight design, which means that, for the considered load, the stresses were at the same level as those generated by the muscle actions. The 2 designs studied demonstrated a gradual distribution of the load from the coronal to the apical region, with a concentration of stress at the neck.

CONCLUSIONS

Stress analysis of 2 different wedge-shaped designs, straight and angled, using the finite element method led to the following conclusions:

- Stresses were generally lower in the angled implant than in the straight implant.
- The differences between the designs studied were more relevant for the vertical load.
- Under the considered loads, both implants presented low stress on the medullary bone area, indicating that the major concentration was actually in the cortical layer, which agrees with previous results.
- A low stress concentration was observed in the apical area for both designs.
- No indication was found that angled implants of the type described generate stress-induced problems compared to straight implants.

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